ENGR 253 LAB #4 - Linear Time-Invariant Systems & Convolution

Objective

Utilize MATLAB to calculate and plot LTI system response with convolution.

Resources

- Signals & Systems textbook by Oppenheim and Willsky
- > Windows running MATLAB release 14 or later
- > USB hard disk or other removable drives (note Lab computer data is lost after reboot)
- Course Lecture Material

Background

- > Calculation of LTI system response using the convolution of input signal and impulse response.
 - Continuous-time $\{y(t) = x(t)^* h(t)\}$

$$y(t) = \int_{-\infty}^{\infty} x(\tau) h(t-\tau) d\tau$$

• Discrete-time $\{y[n] = x[n]^* h[n]\}$

$$y[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$

Conv(A,B)

C = CONV(A, B) convolves vectors A and B. The resulting vector is length LENGTH(A)+LENGTH(B)-1.

Timing Utilities

At times, you are required to analyze the performance of your function. MATLAB offers functions clock() and etime() for determination of elapsed time.

t₁ = clock() returns a 6-element date vector containing the current date and time in decimal form:

 $t_1 = [year month day hour minute seconds]$

- $\circ \quad e = etime(t_2, \, t_1) \text{ returns the time in seconds between date vectors } t_1 \text{ and } t_2.$
- o tic() and toc() functions may provide a more precise approach to timing code in MATLAB.

Experiment #1

Identify the intervals of interest for performing the convolution $\{x[n]^*h[n]\}\$ on the following LTI system. This experiment requires that you write the summations for each interval of interest, but does not require you to simplify the summations.

$$x[n] = h[n] = 3^{n} u[2-n]u[n+10] \longrightarrow y(t)$$

Experiment #2

Utilizing the LTI system definition from Experiment #1, write a MATLAB function that calculates and plots the system response, y[n], to input, x[n], without the use of MATLAB's conv(), fft(), filter() or related functions.

Experiment #3

Utilizing the LTI system definition from Experiment #1, write a MATLAB function that calculates and plots the system response, y[n], to input, x[n], using MATLAB's conv(), fft(), filter() or related functions.

Experiment #4

Compare the function developed in Experiment #2 and #3 including the performance in term of function execution time.

Report Requirements

Reports must be prepared individually even if the experiments are performed as a team. All reports must be computer printed (Formulas and Diagrams may be hand drawn) and at minimum include:

For each Experiment

- a) A clear problem statement; specifying items given and to be found.
- b) Theory or process used.
- c) Resulting circuits, calculation, tables, timing diagram, schematic and other relevant results.

For the report as a whole

- a) Cover sheet with your name, class, lab, completion date and team members' names.
- b) Lessons Learned from the experiments.
- c) A new experiment and expected results which provide additional opportunity to practice the concepts in this lab.